

# Collision Coordinates

Balloons and birds are on a collision course in the sky! When their paths cross, the balloons pop! Plot 10 points for each of the 4 linear equations using the T-charts given. Graph each line on the x-y coordinates and answer the questions on the right.

At what coordinate (x,y) does the orange bird pop the red balloon?

( \_\_ , \_\_ )

At what coordinate (x,y) does the blue bird pop the green balloon?

( \_\_ , \_\_ )

**Red balloon**  
 $y = 2x - 24$

x	y
12	0
13	2

**Green balloon**  
 $y = 3x - 75$

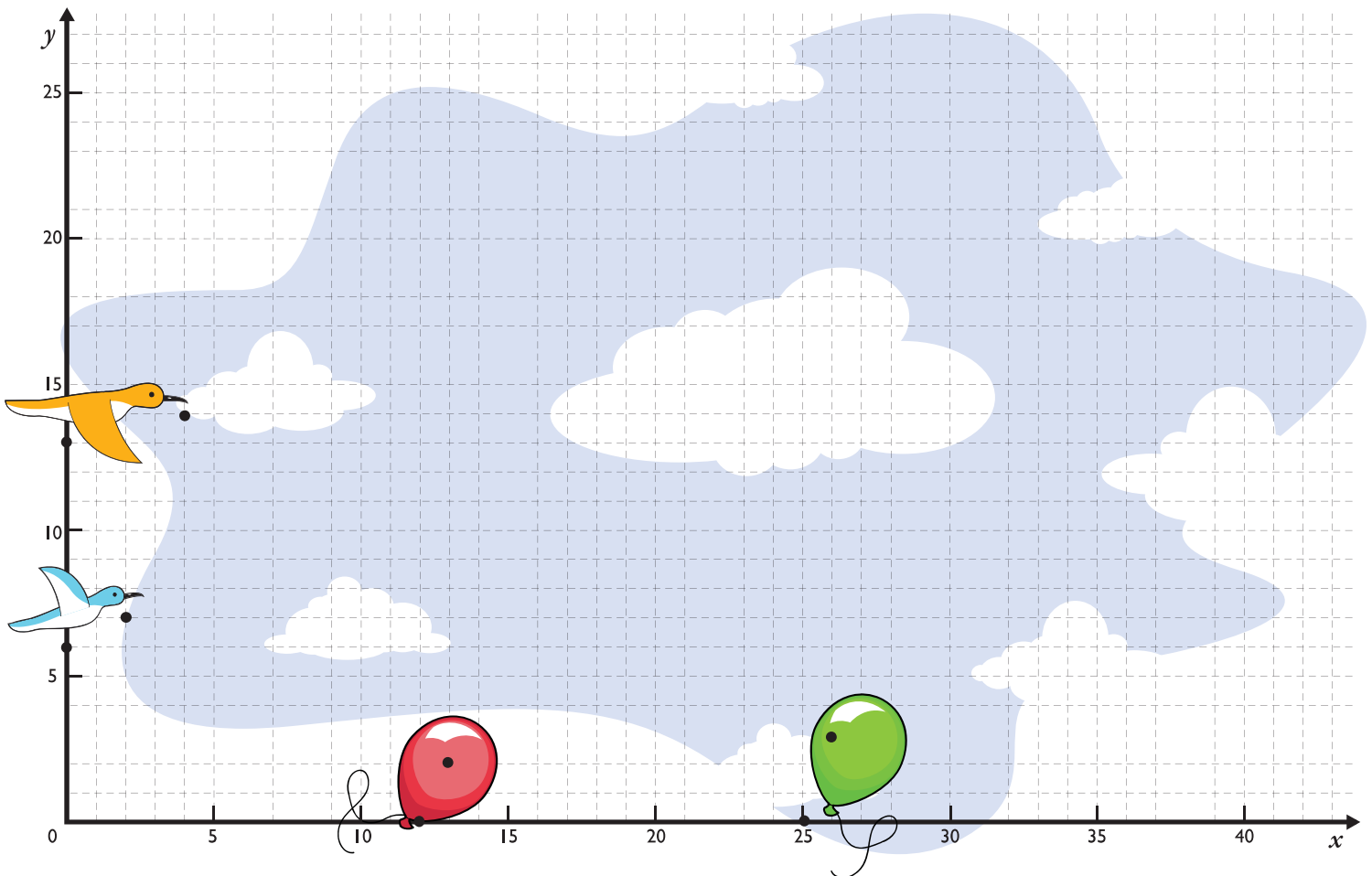
x	y
25	0
26	3

**Orange bird**  
 $y = \frac{x}{2} + 6$

x	y
0	6
2	7

**Blue bird**  
 $y = \frac{x}{4} + 13$

x	y
0	13
4	14



# Greatest Common Factor: Easy

Greatest Common Factor (GCF) is the largest factor that divides two numbers.

*Example:* Find the greatest common factor of 6 and 10.

1. Find the prime factors of each number.

$$6 = 2 \times 3$$

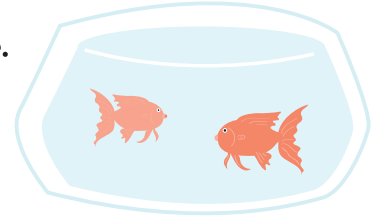
$$10 = 2 \times 5$$

2. Find the common prime factors that 6 and 10 have.

$$6 = 2 \times 3$$

$$10 = 2 \times 5$$

3. The common prime factor of 6 and 10 is 2.



Circle the common factors of the pair of numbers, then answer the questions.

$$4 = 2 \times 2$$

$$6 = 2 \times 3$$

The common prime factor is: \_\_\_\_\_ .

The GCF is \_\_\_\_\_ .

$$6 = 2 \times 3$$

$$9 = 3 \times 3$$

The common prime factor is: \_\_\_\_\_ .

The GCF is \_\_\_\_\_ .

$$10 = 2 \times 5$$

$$12 = 2 \times 2 \times 3$$

The common prime factor is: \_\_\_\_\_ .

The GCF is \_\_\_\_\_ .

$$14 = 2 \times 7$$

$$35 = 5 \times 7$$

The common prime factor is: \_\_\_\_\_ .

The GCF is \_\_\_\_\_ .

Greatest common factor can also be found by *multiplying all the common prime factors*. See the example.

$$18 = 2 \times 3 \times 3$$

$$12 = 2 \times 2 \times 3$$

The common prime factors are 2 and 3 .

The GCF is  $2 \times 3 = 6$  .

$$20 = 2 \times 2 \times 5$$

$$30 = 2 \times 3 \times 5$$

The common prime factors are \_\_\_\_\_ .

The GCF is \_\_\_\_\_ .

Solve the word problems. Show your work and circle your answers.



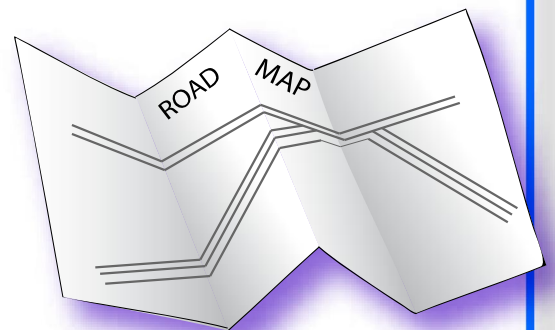
1. Joey and his family are taking a road trip. On Monday, they travel 68 miles. On Tuesday, they travel 25. On Wednesday, they travel 33 miles. What is the average number of miles they drove per day?



2. Joey has three brothers: Jonathan, Jacob, and Jack. Jacob is older than Jonathan but younger than Joey. Jack is younger than Jonathan. List the four boys in order from oldest to youngest.

3. Joey wants to figure out how many minutes his family has spent on the road. On Monday, they traveled for 3 hours. They drove for  $1\frac{1}{2}$  hours on Tuesday and another  $1\frac{1}{2}$  hours on Wednesday. How many minutes have they traveled in all?

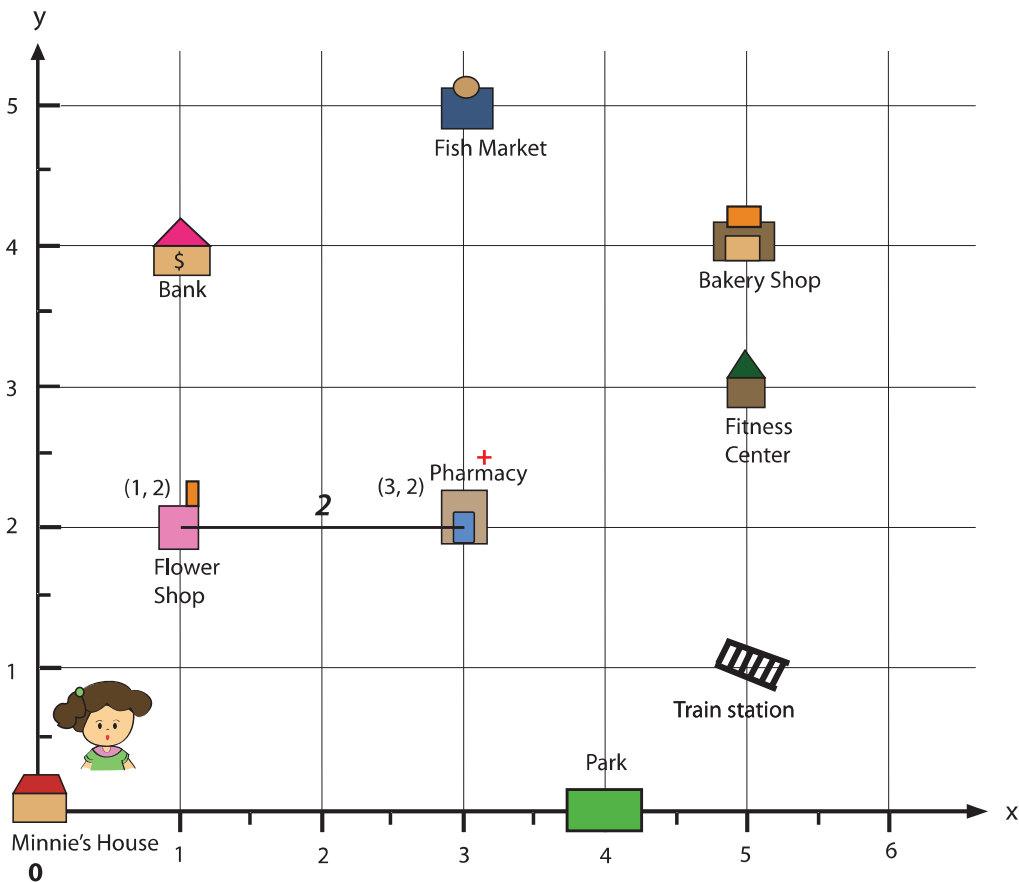
4. Joey and his family plan to visit the Grand Canyon, Yellowstone National Park, and the Washington Monument. They will travel 1,323 miles to get to the Grand Canyon. From there, they'll drive 846 miles to Yellowstone. Finally, they will travel 2,166 miles to get to the Washington Monument. How many miles will they travel altogether?



# Run Errands Efficiently: Practice Coordinates

Help Minnie run errands by telling her how far it is between each location. To find the distances between the coordinates, subtract the x-values and/or the y-values (see an example).

**Review:** The first number refers to X coordinate. The second number refers to Y coordinate.



## Example:

Distance between Pharmacy (3, 2) and Flower shop(1, 2). Subtract difference of X-value of each location. X value of Pharmacy = 3, X value of Flower shop = 1.

Therefore, the distance is  $3 - 1 = 2$ .

1. How far between the pharmacy and the fish market?
2. How far between the bank and the bakery shop?
3. Which one is a greater in distance - Minnie's house to the park, or the train station to the bakery shop?
4. If Minnie travels from the flower shop to the bank, then to the bakery shop, and stops at the fitness center, how far has she traveled?



# Skill Practice 1

## Finding the GCF

✪ The **greatest common factor (GCF)** is the largest whole number that divides evenly into multiple numbers. Look at the two numbers in each problem and find the greatest common factor between them. See the example below for a step by step process to finding the GCF.

### Example

36	48	
2	2	$36 = 18 \times 2$ — 2 is a prime number and divides into 18 evenly 36 times.
2	2	$36 = 9 \times 2 \times 2$ — 18 can be divided by 2, leaving 9.
3	2	$36 = 3 \times 3 \times 2 \times 2$ — 9 can be divided by 3, leaving 3. Now we have all prime numbers.
3	2	$48 = 24 \times 2$
3	2	$48 = 12 \times 2 \times 2$
3	3	$48 = 6 \times 2 \times 2 \times 2$
2	2	$48 = 3 \times 2 \times 2 \times 2 \times 2$
<u><math>2 \times 2 \times 3 = 12</math></u>		Numbers in common: <b>2, 2, 3</b>
GCF		

40	60	30	75	84	105	56	96
GCF		GCF		GCF		GCF	

18	25	50	125	72	108	56	112
GCF		GCF		GCF		GCF	

# Prime Factorization

Factors are numbers that you multiply together to get another number. When a factor is a prime number, it is called a prime factor. For example, the prime factors of 12 are  $2 \times 2 \times 3$ . So 2, 2, and 3 are prime factors of 12.

Find the prime factors of the numbers below. See the example.



$$\begin{aligned}
 16 &= 2 \times 8 \\
 &= 2 \times 2 \times 4 \\
 &= 2 \times 2 \times 2 \times 2
 \end{aligned}$$

$$\begin{aligned}
 36 &= \boxed{4} \times \boxed{9} \\
 &= \boxed{\phantom{00}} \times \boxed{\phantom{00}} \times \boxed{\phantom{00}} \times \boxed{\phantom{00}}
 \end{aligned}$$

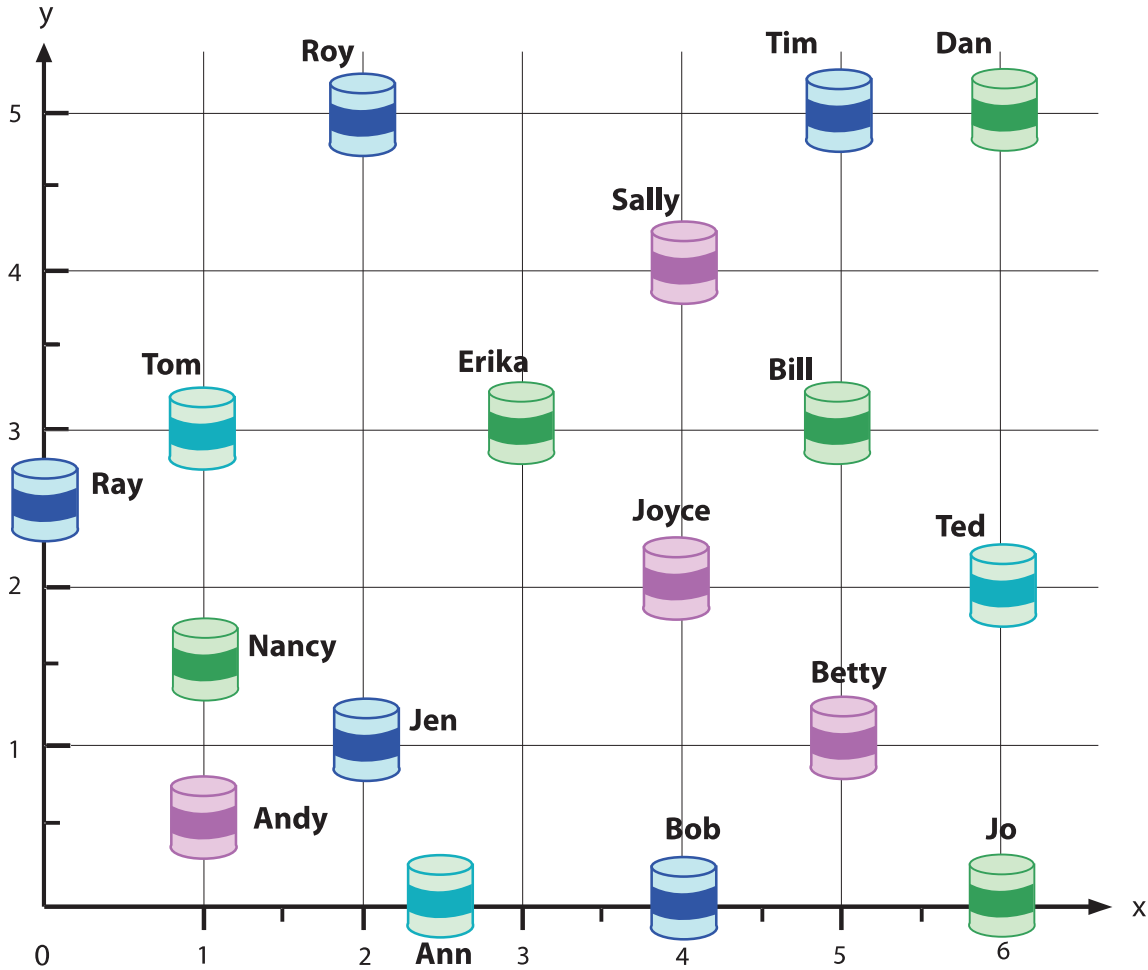
$$\begin{aligned}
 48 &= \boxed{4} \times \boxed{12} \\
 &= \boxed{\phantom{00}} \times \boxed{\phantom{00}} \times \boxed{\phantom{00}} \times \boxed{\phantom{00}} \\
 &= \boxed{\phantom{00}} \times \boxed{\phantom{00}} \times \boxed{\phantom{00}} \times \boxed{\phantom{00}} \times \boxed{\phantom{00}}
 \end{aligned}$$

$$\begin{aligned}
 56 &= \boxed{7} \times \boxed{\phantom{00}} \\
 &= \boxed{\phantom{00}} \times \boxed{\phantom{00}} \times \boxed{\phantom{00}} \\
 &= \boxed{\phantom{00}} \times \boxed{\phantom{00}} \times \boxed{\phantom{00}} \times \boxed{\phantom{00}}
 \end{aligned}$$



# Time Capsules: Practice Coordinates

Your friends need your help in writing code to show where they buried their time capsules, so later they will remember where they are.



Roy = \_\_\_\_\_ Bill = \_\_\_\_\_ Jo = \_\_\_\_\_ Andy = \_\_\_\_\_

Tom = \_\_\_\_\_ Jen = \_\_\_\_\_ Ray = \_\_\_\_\_ Ray = \_\_\_\_\_

Tim = \_\_\_\_\_ Erika = \_\_\_\_\_ Joyce = \_\_\_\_\_ Betty = \_\_\_\_\_

Dan = \_\_\_\_\_ Ann = \_\_\_\_\_ Nancy = \_\_\_\_\_

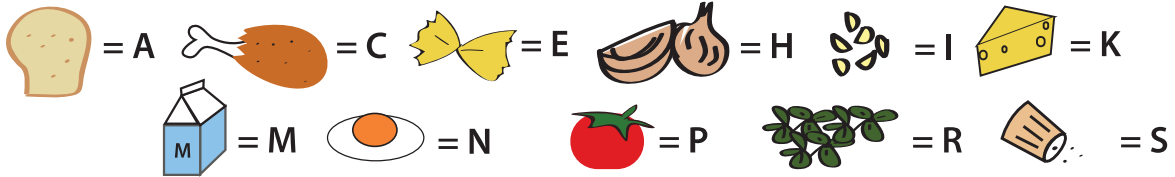
Ted = \_\_\_\_\_ Bob = \_\_\_\_\_ Sally = \_\_\_\_\_



# My Lunch Box: Practice Coordinates

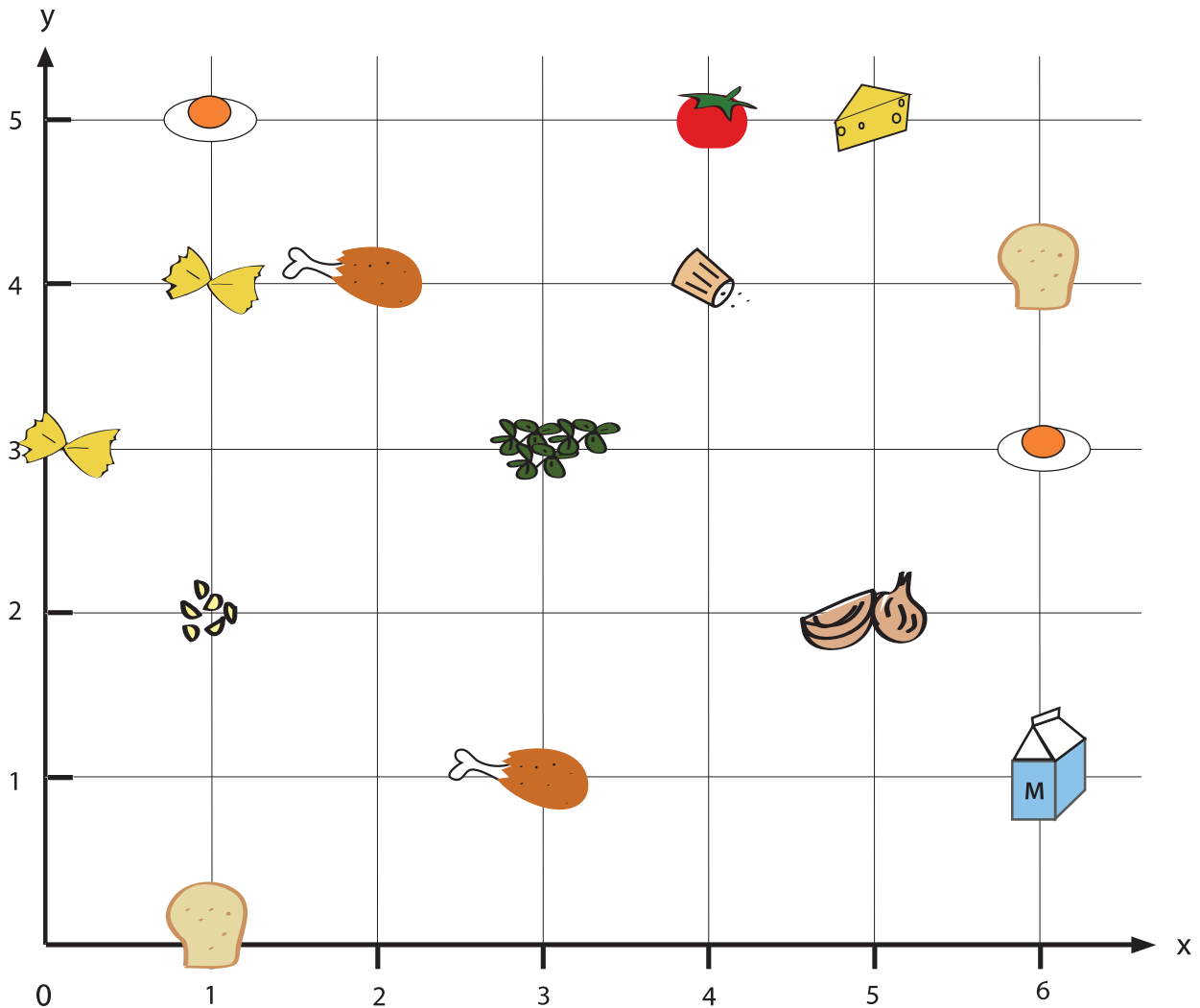
Use the coordinates that go with the ingredients to find the letters that spell out what is in the lunch box.

## Ingredients



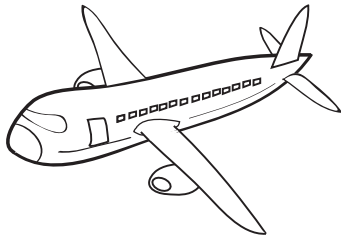
## Coordinates

- |           |           |           |            |            |
|-----------|-----------|-----------|------------|------------|
| 1. (2, 4) | 4. (3, 1) | 7. (6, 3) | 10. (3, 3) | 13. (4, 4) |
| 2. (5, 2) | 5. (5, 5) | 8. (4, 5) | 11. (6, 1) | 14. (6, 4) |
| 3. (1, 2) | 6. (0, 3) | 9. (1, 0) | 12. (1, 4) | 15. (1, 5) |



**Answer:** \_\_\_\_\_





## Air Show: Practice Coordinates

The pilots practice flying skills to prepare for the upcoming air show. Help each pilot organize his positions by plotting his coordinates in the grid below and drawing a line to connect each dot of his route. Use a different color for each pilot.

### Pilot A

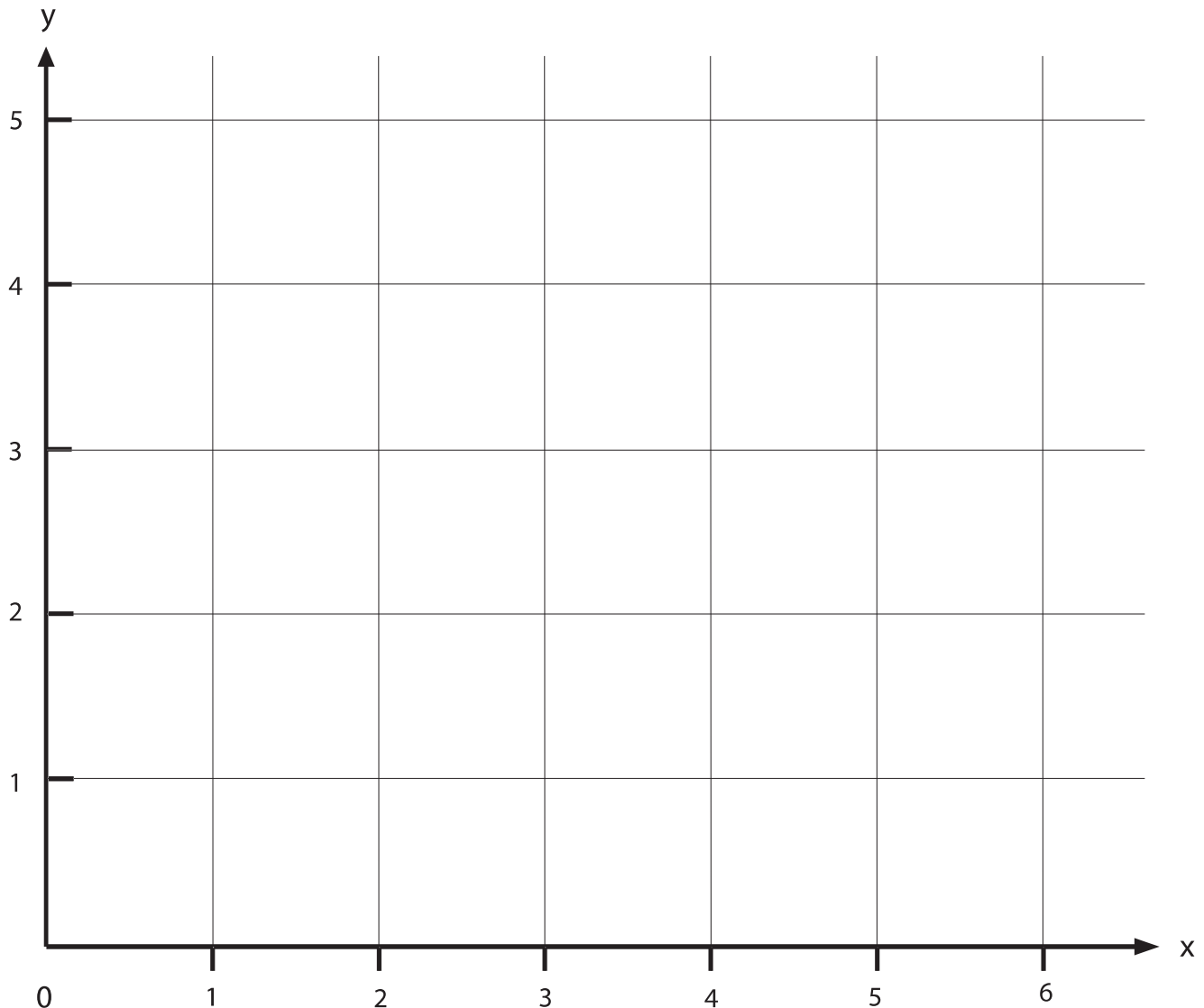
1. (0, 5)
2. (2, 4)
3. (2, 3)
4. (4, 2)
5. (4, 1)
6. (5, 2)

### Pilot B

1. (2.5, 4.5)
2. (5, 4)
3. (3, 3)
4. (6, 3)
5. (5, 5)
6. (6, 3.5)

### Pilot C

1. (1.5, 4)
2. (1, 2)
3. (2, 2.5)
4. (3, 0.5)
5. (5, 0)
6. (6, 2)



# Least Common Multiple: Hard



A *multiple* is the product of two integers. To find the multiples of a certain number, multiply that number by every integer, starting with 1.

*Example:* Multiples of 10 are 10, 20, 30, 40, 50, and so on.

*Common multiples* are numbers that share two or more of the same multiples.

*Example:* Multiples of 10 are 10, 20, 30, 40, 50, 60, and so on.

Multiples of 15 are 15, 30, 45, 60, 75, and so on.

30 and 60 appears in these lists, so they are common multiples of 10 and 15.

*Least common multiple (LCM)* is the smallest common multiple of two or more numbers.

From the example above, the LCM of 10 and 15 is 30.

LCM can be found by listing all the multiples and looking for the smallest common one in the lists.

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Find the least common multiple of numbers below. Follow the directions.

Multiples of 9 = 9, 18, , , , , ...

Multiples of 15 = 15, 30, , , , , ...

The common multiple is \_\_\_\_\_ . The LCM is \_\_\_\_\_ .

Multiples of 20 = , , , , , , ...

Multiples of 30 = , , , , , , ...

The common multiples are \_\_\_\_\_ . The LCM is \_\_\_\_\_ .

Multiples of 10 = , , , , , , ...

Multiples of 20 = , , , , , , ...

Multiples of 50 = , , , , , , ...

The common multiples are \_\_\_\_\_ . The LCM is \_\_\_\_\_ .

# Greatest Common Factor: Hard

Greatest Common Factor (GCF) is the largest factor that divides two numbers.

*Example:* Find the greatest common factor of 24 and 18.

1. Find the prime factors of each number.

$$24 = 6 \times 4 = 2 \times 3 \times 2 \times 2$$

$$18 = 6 \times 3 = 2 \times 3 \times 3$$

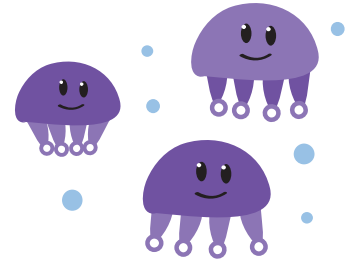
2. Find the common prime factors of 24 and 18.

$$24 = 2 \times 3 \times 2 \times 2$$

$$18 = 2 \times 3 \times 3$$

3. The common prime factors of 24 and 18 are 2 and 3.

The greatest common factor can be found by *multiplying all the common prime factors*. Therefore, the greatest common factor of 24 and 18 is  $2 \times 3 = 6$ .



Find the greatest common factor of the numbers below.

$$30 = 3 \times \quad \times \quad$$

$$45 = 3 \times 3 \times \quad$$

The common prime factors are:                     . The GCF is                     .

$$36 = 3 \times 2 \times 2 \times \quad$$

$$42 = 7 \times \quad \times 3$$

The common prime factors are:                     . The GCF is                     .

$$120 = 2 \times \quad \times 3 \times 5 \times \quad$$

$$100 = 2 \times 5 \times \quad \times \quad$$

The common prime factors are:                     . The GCF is                     .