

GIỚI HẠN KHI $x \rightarrow \pm\infty$ TÓI VÔ CỰC

Câu 1: Tìm các giới hạn sau:

$$\begin{array}{lll} \text{a). } \lim_{x \rightarrow -\infty} \frac{3x^2 - x + 7}{2x^3 - 1} & \text{b). } \lim_{x \rightarrow +\infty} \frac{(4x^2 + 1)(7x - 1)}{(2x^3 - 1)(x + 3)} & \text{c). } \lim_{x \rightarrow +\infty} \frac{x\sqrt{x+3}}{x^2 - x + 2} \\ \text{d). } \lim_{x \rightarrow +\infty} \left[(x+1) \sqrt{\frac{x}{2x^4 + x^2 + 1}} \right] & \text{e). } \lim_{x \rightarrow -\infty} x \sqrt{\frac{2x^3 + x}{x^5 - x^2 + 3}}. \end{array}$$

LỜI GIẢI

$$\text{a). } \lim_{x \rightarrow -\infty} \frac{3x^2 - x + 7}{2x^3 - 1} = \lim_{x \rightarrow -\infty} \frac{x^2 \left(3 - \frac{1}{x} + \frac{7}{x^2} \right)}{x^3 \left(2 - \frac{1}{x^3} \right)} = \lim_{x \rightarrow -\infty} \frac{3 - \frac{1}{x} + \frac{7}{x^2}}{x \left(2 - \frac{1}{x^3} \right)} = \lim_{x \rightarrow -\infty} \frac{3}{2x} = 0$$

$$\text{b). } \lim_{x \rightarrow +\infty} \frac{(4x^2 + 1)(7x - 1)}{(2x^3 - 1)(x + 3)} = \lim_{x \rightarrow +\infty} \frac{x^2 \left(4 + \frac{1}{x^2} \right) x \left(7 - \frac{1}{x} \right)}{x^3 \left(2 - \frac{1}{x^3} \right) x \left(1 + \frac{3}{x} \right)} = \lim_{x \rightarrow +\infty} \frac{\left(4 + \frac{1}{x^2} \right) \left(7 - \frac{1}{x} \right)}{x \left(2 - \frac{1}{x^3} \right) \left(1 + \frac{3}{x} \right)} = \lim_{x \rightarrow +\infty} \frac{28}{2x} = 0$$

$$\text{c). } \lim_{x \rightarrow +\infty} \frac{x\sqrt{x+3}}{x^2 - x + 2} = \lim_{x \rightarrow +\infty} \frac{x\sqrt{x} \left(1 + \frac{3}{x\sqrt{x}} \right)}{x^2 \left(1 - \frac{1}{x} + \frac{2}{x^2} \right)} = \lim_{x \rightarrow +\infty} \frac{1 + \frac{3}{x\sqrt{x}}}{\sqrt{x} \left(1 - \frac{1}{x} + \frac{2}{x^2} \right)} = \lim_{x \rightarrow +\infty} \frac{1}{\sqrt{x}} = 0.$$

$$\begin{aligned} \text{d). } \lim_{x \rightarrow +\infty} \left[(x+1) \sqrt{\frac{x}{2x^4 + x^2 + 1}} \right] &= \lim_{x \rightarrow +\infty} \left[(x+1) \sqrt{\frac{x}{x^4 \left(2 + \frac{1}{x^2} + \frac{1}{x^4} \right)}} \right] \\ &= \lim_{x \rightarrow +\infty} \left[(x+1) \sqrt{\frac{1}{2x^3}} \right] = \lim_{x \rightarrow +\infty} \left[(x+1) \frac{1}{x\sqrt{x}\sqrt{2}} \right] = \lim_{x \rightarrow +\infty} \left[x \left(1 + \frac{1}{x} \right) \frac{1}{x\sqrt{x}\sqrt{2}} \right] = 0 \end{aligned}$$

$$\text{e). } \lim_{x \rightarrow -\infty} x \sqrt{\frac{2x^3 + x}{x^5 - x^2 + 3}} = \lim_{x \rightarrow -\infty} x \sqrt{\frac{x^3 \left(x + \frac{1}{x^2} \right)}{x^5 \left(1 - \frac{1}{x^3} + \frac{3}{x^5} \right)}} = \lim_{x \rightarrow -\infty} x \frac{\sqrt{2}}{\sqrt{x^2}} = \lim_{x \rightarrow -\infty} x \frac{\sqrt{2}}{|x|} = \lim_{x \rightarrow -\infty} x \frac{\sqrt{2}}{-x} = -\sqrt{2}$$